

(1) A finite length ( $N=4$ ) signal consists of the sequence:  $x[n] = \{1 \ 0 \ 2 \ -1\}$ . Determine the DFT sequence  $X[k]$  for  $k=0, 1, 2, 3$ .

(2) What is the relationship between the length 4 DFT of the sequence  $\{1 \ 2 \ 3 \ 1\}$  and the length 8 DFT of the sequence  $\{1 \ 2 \ 3 \ 1 \ 0 \ 0 \ 0 \ 0\}$ ? Explain.

(3) An IIR difference equation is given:  $y[n] = 0.5 y[n-1] + x[n]$

Assuming initial rest, what is the functional form for the output signal  $y[n]$  if the input signal is a unit step? Use the inverse z-transform method.